האוניברסיטה העברית בירושלים THE HEBREW UNIVERSITY OF JERUSALEM



The Hebrew University of Jerusalem

Syllabus

DISCRETE MATHEMATICS for Odyssey program - 49680

Last update 04-04-2025

HU Credits: 5

Degree/Cycle: 1st degree (Bachelor)

Responsible Department: Young Scientist

Academic year: 0

Semester: 2nd Semester

<u>Teaching Languages:</u> Hebrew

Campus: E. Safra

Course/Module Coordinator: Dr. Alex Gourevich

Coordinator Email: youth@math.huji.ac.il

Coordinator Office Hours:

Teaching Staff:

Dr. Alex Gourevich, Mr. Ben Baskin

Course/Module description:

1. Logic – Boolean operations, truth tables, propositional calculus and semantic 2. Set theory – operations on sets, Cartesian product, functions

3. Relations - equivalence and order relations, partially ordered sets

4. Counting problems - counting with and without order importance, set partitions

5. Identities - the binomial and multinomial formulas, combinatorial and algebraic proofs

6. Reflection method - Catalan numbers

7. Inclusion-exclusion principal – enumeration surjective maps, enumeration permutations without fixed point, Euler's function

8. Induction and recursion – proofs by complete induction, solving of combinatorial problems with the aid of recursion, Fibonacci numbers

9. Pigeonhole principle - Erdos-Szekeres theorem

10.Asymptotic analysis - asymptotic analysis of combinatorial problems

11. Graphs – paths, connectivity, cycles, trees, bipartite graphs, Eulerian trails and cycles, Hamiltonian trails and cycles, matching, Hall's marriage theorem, colored graphs, Ramsey theory

Additional topics may be studied.

Course/Module aims:

Providing basic notions of Discrete Math and developing the ability to solve problems.

Learning outcomes - On successful completion of this module, students should be able to:

Solve elementary problems in set theory, combinatorics, and graph theory.

<u>Attendance requirements(%):</u> 80%

Teaching arrangement and method of instruction: lecture + exercise session

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<u>Required Reading:</u> none

Additional Reading Material:

<u>Grading Scheme:</u> Written / Oral / Practical Exam 90 % Submission assignments during the semester: Exercises / Essays / Audits / Reports / Forum / Simulation / others 10 %

Additional information: